

William Navidi $\leftrightarrow$ Barry Monk


## Second Edition

## Essential STATISTICS

$\underset{\text { Colorado School of Mines }}{\text { William }} \otimes \quad \begin{aligned} & \text { Barry Monk Middle Georgia State University }\end{aligned}$

## ELEMENTARY STATISTICS, SECOND EDITION

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# To Catherine, Sarah, and Thomas <br> —William Navidi 

$$
\begin{aligned}
& \text { To Shaun, Dawn, and Ben } \\
& \text {-Barry Monk }
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## About the Authors



William Navidi is a professor of Applied Mathematics and Statistics at the Colorado School of Mines in Golden, Colorado. He received a Bachelor's degree in Mathematics from New College, a Master's degree in Mathematics from Michigan State University, and a Ph.D. in Statistics from the University of California at Berkeley. Bill began his teaching career at the County College of Morris, a two-year college in Dover, New Jersey. He has taught mathematics and statistics at all levels, from developmental through the graduate level. Bill has written two Engineering Statistics textbooks for McGraw-Hill. In his spare time, he likes to play racquetball.


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## Preface

This book is designed for an introductory course in statistics. The mathematical prerequisite is basic algebra. In addition to presenting the mechanics of the subject, we have endeavored to explain the concepts behind them in a writing style as straightforward, clear, and engaging as we could make it. As practicing statisticians, we have done everything possible to ensure that the material is accurate and correct. We believe that this book will enable instructors to explore statistical concepts in depth yet remain easy for students to read and understand.

To achieve this goal, we have incorporated a number of useful pedagogical features:

## Features

- Check Your Understanding Exercises: After each concept is explained, one or more exercises are immediately provided for students to be sure they are following the material. These exercises provide students with confidence that they are ready to go on, or alert them to the need to review the material just covered.
- Explain It Again: Many important concepts are reinforced with additional explanation in these marginal notes.
- Real Data: Statistics instructors universally agree that the use of real data engages students and convinces them of the usefulness of the subject. A great many of the examples and exercises use real data. Some data sets explore topics in health or social sciences, while others are based in popular culture such as movies, contemporary music, or video games.
- Integration of Technology: Many examples contain screenshots from the TI-84 Plus calculator, MINITAB, and Excel. Each section contains detailed, step-by-step instructions, where applicable, explaining how to use these forms of technology to carry out the procedures explained in the text.
- Interpreting Technology: Many exercises present output from technology and require the student to interpret the results.
- Write About It: These exercises, found at the end of each chapter, require students to explain statistical concepts in their own words.
- Case Studies: Each chapter begins with a discussion of a real problem. At the end of the chapter, a case study demonstrates applications of chapter concepts to the problem.


## Flexibility

We have endeavored to make our book flexible enough to work effectively with a wide variety of instructor styles and preferences. We cover both the $P$-value and critical value approaches to hypothesis testing, so instructors can choose to cover either or both of these methods.

Instructors differ in their preferences regarding the depth of coverage of probability. A light treatment of the subject may be obtained by covering Section 4.1 and skipping the rest of the chapter. More depth can be obtained by covering Section 4.2.

## Supplements

Supplements, including online homework, videos, and PowerPoint presentations, play an increasingly important role in the educational process. As authors, we have adopted a hands-on approach to the development of our supplements, to make sure that they are consistent with the style of the text and that they work effectively with a variety of instructor preferences. In particular, our online homework package offers instructors the flexibility to choose whether the solutions that students view are based on tables or technology, where applicable.

## New in This Edition

The second edition of the book is intended to extend the strengths of the first. Some of the changes are:

- The material introducing the normal distribution has been rewritten to make it equally accessible for those using tables or technology.
- The material on percentiles and quantiles has been rewritten to make it easier for those who wish to cover quantiles without covering percentiles.
- A large number of new exercises have been included, many of which involve real data from recent sources.
- Several of the case studies have been updated.
- The exposition has been improved in a number of places.


## Feedback from Statistics Instructors

Paramount to the development of Essential Statistics was the invaluable feedback provided by the instructors from around the country who reviewed the manuscript while it was in development.

Over 150 instructors reviewed the manuscript from the first draft through the final manuscript, providing feedback to the authors at each stage of development.
AnsrSource accuracy checked every worked example and exercise in the text numerous times, both in the final phase of the manuscript and in the page proof stages.
Focus groups and symposia were conducted with instructors from around the country to provide feedback to editors and the authors to ensure the direction of the text was meeting the needs of students and instructors.

## A Special Thanks to All of the Symposia and Focus Group <br> Attendees Who Helped Shape Essential Statistics, First and Second Editions

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The staff at McGraw-Hill has been extremely capable and supportive. Project Manager Peggy Selle was always patient and helpful. Rob Brieler was superb in directing the development of our digital content. We owe a debt of thanks to Sally Yagan, for her creative marketing and diligence in spreading the word about our book. We appreciate the guidance of our editors, Ryan Blankenship, Adam Rooke, and Christina Sanders, whose input has considerably improved the final product.

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## MegaStat ${ }^{\circledR}$

MegaStat ${ }^{\circledR}$ is a statistical add-in for Microsoft Excel, handcrafted by J. B. Orris of Butler University. When MegaStat is installed, it appears as a menu item on the Excel menu bar and allows you to perform statistical analysis on data in an Excel workbook.

## Computerized Test Bank (CTB) Online (instructors only)

The computerized test bank contains a variety of questions, including true/false, multiplechoice, short-answer, and short problems requiring analysis and written answers. The testing material is coded by type of question and level of difficulty. It also allows for printing tests along with answer keys as well as editing the original questions, and it is available for Windows and Macintosh systems. Printable tests and a print version of the test bank can also be found on the website.

## Videos

Videos by the authors introduce concepts, definitions, theorems, formulas, and problemsolving procedures to help students comprehend topics throughout the text. They show students how to work through selected exercises, following methodology employed in the text. These videos are closed-captioned for the hearing-impaired, are subtitled in Spanish, and meet the Americans with Disabilities Act Standards for Accessible Design.

## SPSS Student Version for Windows

A student version of SPSS statistical software is available with copies of this text. Consult your McGraw-Hill representative for details.

## Instructor's Solution Manual

Derived from author solutions, this manual contains detailed solutions to all of the problems in the text.

## Guided Student Notes

Guided notes provide instructors with the framework of day-by-day class activities for each section in the book. Each lecture guide can help instructors make more efficient use of class time and can help keep students focused on active learning. Students who use the lecture guides have the framework of well-organized notes that can be completed with the instructor in class.

## Data Sets

Data sets from selected exercises have been pre-populated into MINITAB, TI-Graph Link, Excel, SPSS, and comma-delimited ASCII formats for student and instructor use. These files are available on the text's website.

## MINITAB 17 Manual

With guidance from the authors, this manual includes material from the book to provide seamless use from one to the other, providing additional practice in applying the chapter concepts while using the MINITAB program.

## TI-84 Plus Graphing Calculator Manual

This friendly, author-influenced manual teaches students to learn about statistics and solve problems by using this calculator while following each text chapter.

## Excel Manual

This workbook, specially designed to accompany the text by the authors, provides additional practice in applying the chapter concepts while using Excel.

## Print Supplements

## Annotated Instructor's Edition (instructors only)

The Annotated Instructor's Edition contains answers to all exercises. The answers to most questions are printed in blue next to each problem. Answers not appearing on the page can be found in the Answer Appendix at the end of the book.

## Student's Solution Manual

Derived from author solutions, this manual contains detailed solutions to all odd-numbered text problems and answers to all Quizzes, Reviews, and Case Study problems found at the end of each chapter.

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U.S. Fish \& Wildlife Service

## Basic Ideas

## Introduction

How does air pollution affect your health? Over the past several decades, scientists have become increasingly convinced that air pollution is a serious health hazard. The World Health Organization has estimated that air pollution causes 2.4 million deaths each year. The health effects of air pollution have been investigated by measuring air pollution levels and rates of disease, then using statistical methods to determine whether higher levels of pollution lead to higher rates of disease.

Many air pollution studies have been conducted in the United States. For example, the town of Libby, Montana, was the focus of a recent study of the effect of particulate matter - air pollution that consists of microscopic particles - on the respiratory health of children. As part of this study, parents were asked to fill out a questionnaire about their children's respiratory symptoms. It turned out that children exposed to higher levels of particulate pollution were more likely to exhibit symptoms of wheezing, as shown in the following table.

| Level of Exposure | Percentage with Symptoms |
| :---: | :---: |
| High | $8.89 \%$ |
| Low | $4.56 \%$ |

The rate of symptoms was almost twice as high among those exposed to higher levels of pollution. At first, it might seem easy to conclude that higher levels of pollution cause symptoms of wheezing. However, drawing accurate conclusions from information like this is rarely that simple. The case study at the end of this chapter will present more complete information and will show that additional factors must be considered.

## Objectives

## 1. Construct a simple random sample

2. Determine when samples of convenience are acceptable
3. Describe stratified sampling, cluster sampling, systematic sampling, and voluntary response sampling
4. Distinguish between statistics and parameters

In the months leading up to an election, polls often tell us the percentages of voters that prefer each of the candidates. How do pollsters obtain this information? The ideal poll would be one in which every registered voter were asked his or her opinion. Of course, it is impossible to conduct such an ideal poll, because it is impossible to contact every voter. Instead, pollsters contact a relatively small number of voters, usually no more than a couple of thousand, and use the information from these voters to predict the preferences of the entire group of voters.

The process of polling requires two major steps. First, the voters to be polled must be selected and interviewed. In this way the pollsters collect information. In the second step, the pollsters analyze the information to make predictions about the upcoming election. Both the collection and the analysis of the information must be done properly for the results to be reliable. The field of statistics provides appropriate methods for the collection, description, and analysis of information.

## DEFINITION

Statistics is the study of procedures for collecting, describing, and drawing conclusions from information.

The polling problem is typical of a problem in statistics. We want some information about a large group of individuals, but we are able to collect information on only a small part of that group. In statistical terminology, the large group is called a population, and the part of the group on which we collect information is called a sample.

## Explain It Again

Why do we draw samples?
It's usually impossible to examine every member of a large population. So we select a group of a manageable size to examine. This group is called a sample.

## DEFINITION

- A population is the entire collection of individuals about which information is sought.
- A sample is a subset of a population, containing the individuals that are actually observed.

Ideally, we would like our sample to represent the population as closely as possible. For example, in a political poll, we would like the proportions of voters preferring each of the candidates to be the same in the sample as in the population. Unfortunately, there are no methods that can guarantee that a sample will represent the population well. The best we can do is to use a method that makes it very likely that the sample will be similar to the population. The best sampling methods all involve some kind of random selection. The most basic, and in many cases the best, sampling method is the method of simple random sampling.

## Simple Random Sampling

To understand the nature of a simple random sample, think of a lottery. Imagine that 10,000 lottery tickets have been sold, and that 5 winners are to be chosen. What is the fairest way to choose the winners? The fairest way is to put the 10,000 tickets in a drum, mix them thoroughly, then reach in and draw 5 tickets out one by one. These 5 winning tickets are a simple random sample from the population of 10,000 lottery tickets. Each ticket is equally likely to be one of the 5 tickets drawn. More importantly, each collection of 5 tickets that can be formed from the 10,000 is equally likely to comprise the group of 5 that is drawn.

## DEFINITION

A simple random sample of size $n$ is a sample chosen by a method in which each collection of $n$ population items is equally likely to make up the sample, just as in a lottery.

Since a simple random sample is analogous to a lottery, it can often be drawn by the same method now used in many lotteries: with a computer random number generator. Suppose there are $N$ items in the population. We number the items 1 through $N$. Then we generate a list of random integers between 1 and $N$, and choose the corresponding population items to comprise the simple random sample.

## EXAMPLE 1.1 Choosing a simple random sample

There are 300 employees in a certain company. The Human Resources department wants to draw a simple random sample of 20 employees to fill out a questionnaire about their attitudes toward their jobs. Describe how technology can be used to draw this sample.

## Solution

Step 1: Make a list of all 300 employees, and number them from 1 to 300.
Step 2: Use a random number generator on a computer or a calculator to generate 20 random numbers between 1 and 300 . The employees who correspond to these numbers comprise the sample.

## EXAMPLE 1.2 Determining whether a sample is a simple random sample

A physical education professor wants to study the physical fitness levels of students at her university. There are 20,000 students enrolled at the university, and she wants to draw a sample of size 100 to take a physical fitness test. She obtains a list of all 20,000 students, numbered from 1 to 20,000 . She uses a computer random number generator to generate 100 random integers between 1 and 20,000, then invites the 100 students corresponding to those numbers to participate in the study. Is this a simple random sample?

## Solution

Yes, this is a simple random sample because any group of 100 students would have been equally likely to have been chosen.

## EXAMPLE 1.3 Determining whether a sample is a simple random sample

The professor in Example 1.2 now wants to draw a sample of 50 students to fill out a questionnaire about which sports they play. The professor's 10:00 A.M. class has 50 students. She uses the first 20 minutes of class to have the students fill out the questionnaire. Is this a simple random sample?

## Solution

No. A simple random sample is like a lottery, in which each student in the population has an equal chance to be part of the sample. In this case, only the students in a particular class had a chance to be in the sample.

## EXAMPLE 1.4 In a simple random sample, all samples are equally likely

To play the Colorado Lottery Lotto game, you must select six numbers from 1 to 42 . Then lottery officials draw a simple random sample of six numbers from 1 to 42 . If your six numbers match the ones in the simple random sample, you win the jackpot. Sally plays the lottery

## EXAMPLE 1.5 Using technology to draw a simple random sample

Use technology to draw a simple random sample of five employees from the following list.

| 1. Dan Aaron | 11. Johnny Gaines | 21. Jorge Ibarra | 31. Edward Shingleton |
| :--- | :--- | :--- | :--- |
| 2. Annie Bienh | 12. Carlos Garcia | 22. Maurice Jones | 32. Michael Speciale |
| 3. Oscar Bolivar | 13. Julio Gonzalez | 23. Jared Kerns | 33. Andrew Steele |
| 4. Dominique Bonnaud | 14. Jacqueline Gordon | 24. Kevin King | 34. Neil Swain |
| 5. Paul Campbell | 15. James Graves | 25. Frank Lipka | 35. Sherry Thomas |
| 6. Jeffrey Carnahan | 16. Ronald Harrison | 26. Carl Luther | 36. Shequiea Thompson |
| 7. Joel Chae | 17. Andrew Huang | 27. Laverne Mitchell | 37. Barbara Tilford |
| 8. Dustin Chen | 18. Anthony Hunter | 28. Zachary Quesada | 38. Jermaine Tryon |
| 9. Steven Coleman | 19. Jonathan Jackson | 29. Donnell Romaine | 39. Lizbet Valdez |
| 10. Richard Davis | 20. Bruce Johnson | 30. Gary Sanders | 40. Katelyn Yu |

## Solution

We will use the TI-84 Plus graphing calculator. The step-by-step procedure is presented in the Using Technology section on page 9 . We begin by choosing a seed, which is a number that the calculator uses to get the random number generator started. Display (a) shows the seed being set to 21 . (The seed can be chosen in almost any way; this number was chosen by looking at the seconds display on a digital watch.) Display (b) presents the five numbers in the sample.


The simple random sample consists of the employees with numbers $27,39,30,35$, and 17. These are Laverne Mitchell, Lizbet Valdez, Gary Sanders, Sherry Thomas, and Andrew Huang.

## Check Your Understanding

1. A pollster wants to estimate the proportion of voters in a certain town who are Democrats. He goes to a large shopping mall and approaches people to ask whether they are Democrats. Is this a simple random sample? Explain.
2. A telephone company wants to estimate the proportion of customers who are satisfied with their service. They use a computer to generate a list of random phone numbers and call those people to ask them whether they are satisfied. Is this a simple random sample? Explain.

## Objective 2 Determine when samples of convenience are acceptable

## EXAMPLE 1.6


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## CAUTION

Don't use a sample of convenience when it is possible to draw a simple random sample.

## Samples of Convenience

In some cases, it is difficult or impossible to draw a sample in a truly random way. In these cases, the best one can do is to sample items by some convenient method. A sample obtained in such a way is called a sample of convenience.

## DEFINITION

A sample of convenience is a sample that is not drawn by a well-defined random method.

## Drawing a sample of convenience

A construction engineer has just received a shipment of 1000 concrete blocks, each weighing approximately 50 pounds. The blocks have been delivered in a large pile. The engineer wishes to investigate the crushing strength of the blocks by measuring the strengths in a sample of 10 blocks. Explain why it might be difficult to draw a simple random sample of blocks. Describe how the engineer might draw a sample of convenience.

## Solution

To draw a simple random sample would require removing blocks from the center and bottom of the pile, which might be quite difficult. One way to draw a sample of convenience would be to simply take 10 blocks off the top of the pile.

## Problems with samples of convenience

The big problem with samples of convenience is that they may differ systematically in some way from the population. For this reason, samples of convenience should not be used, except in some situations where it is not feasible to draw a random sample. When it is necessary to draw a sample of convenience, it is important to think carefully about all the ways in which the sample might differ systematically from the population. If it is reasonable to believe that no important systematic difference exists, then it may be acceptable to treat the sample of convenience as if it were a simple random sample. With regard to the concrete blocks, if the engineer is confident that the blocks on the top of the pile do not differ systematically in any important way from the rest, then he can treat the sample of convenience as a simple random sample. If, however, it is possible that blocks in different parts of the pile may have been made from different batches of mix, or may have different curing times or temperatures, a sample of convenience could give misleading results.

## SUMMARY

- A sample of convenience may be acceptable when it is reasonable to believe that there is no systematic difference between the sample and the population.
- A sample of convenience is not acceptable when it is possible that there is a systematic difference between the sample and the population.


## Some Other Sampling Methods <br> \section*{Stratified sampling}

In stratified sampling, the population is divided into groups, called strata, where the members of each stratum are similar in some way. Then a simple random sample is drawn from each stratum. Stratified sampling is useful when the strata differ from one another, but the individuals within a stratum tend to be alike.

## EXAMPLE 1.7 Drawing a stratified sample

A company has 1000 employees, of whom 800 are full-time and 200 are part-time. The company wants to survey 50 employees about their opinions regarding benefits. Attitudes toward benefits may differ considerably between full-time and part-time employees. Why might it be a good idea to draw a stratified sample? Describe how one might be drawn.

## Solution

If a simple random sample is drawn from the entire population of 1000 employees, it is possible that the sample will contain only a few part-time employees, and their attitudes will not be well represented. For this reason, it might be advantageous to draw a stratified sample. To draw a stratified sample, one would use two strata. One stratum would consist of the full-time employees, and the other would consist of the part-time employees. A simple random sample would be drawn from the full-time employees, and another simple random sample would be drawn from the part-time employees. This method guarantees that both full-time and part-time employees will be well represented.

## Explain It Again

Example of a cluster sample: Imagine drawing a simple random sample of households, and interviewing every member of each household. This would be a cluster sample, with the households as the clusters.

## EXAMPLE 1.8 Drawing a cluster sample

To estimate the unemployment rate in a county, a government agency draws a simple random sample of households in the county. Someone visits each household and asks how many adults live in the household, and how many of them are unemployed. What are the clusters? Why is this a cluster sample?

## Solution

The clusters are the groups of adults in each of the households in the county. This a cluster sample because a simple random sample of clusters is selected, and every individual in each selected cluster is part of the sample.

## Explain It Again

The difference between cluster sampling and stratified sampling: In both cluster sampling and stratified sampling, the population is divided into groups. In stratified sampling, a simple random sample is chosen from each group. In cluster sampling, a random sample of groups is chosen, and every member of the chosen groups is sampled.

## Systematic sampling

Imagine walking alongside a line of people and choosing every third one. That would produce a systematic sample. In a systematic sample, the population items are ordered. It is decided how frequently to sample items; for example, one could sample every third item, or every fifth item, or every hundredth item. Let $k$ represent the sampling frequency. To begin the sampling, choose a starting place at random. Select the item in the starting place, along with every $k$ th item after that.

Systematic sampling is sometimes used to sample products as they come off an assembly line, in order to check that they meet quality standards.

## EXAMPLE 1.9 Describe a systematic sample

Automobiles are coming off an assembly line. It is decided to draw a systematic sample for a detailed check of the steering system. The starting point will be the third car, then every fifth car after that will be sampled. Which cars will be sampled?

## Solution


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We start with the third car, then count by fives to determine which cars will be sampled. The sample will consist of cars numbered $3,8,13,18$, and so on.

## Voluntary response sampling

Voluntary response samples are often used by the media to try to engage the audience. For example, a news commentator will invite people to tweet an opinion, or a radio announcer will invite people to call the station to say what they think. How reliable are voluntary response samples? To put it simply, voluntary response samples are never reliable. People who go to the trouble to volunteer an opinion tend to have stronger opinions than is typical of the population. In addition, people with negative opinions are often more likely to volunteer their responses than those with positive opinions.

Figures 1.1-1.4 illustrate several valid methods of sampling.


Figure 1.1 Simple random sampling


Figure 1.3 Stratified sampling


Figure 1.2 Systematic sampling


Figure 1.4 Cluster sampling

## Check Your Understanding

3. A radio talk-show host invites listeners to send an email to express their opinions on an upcoming election. More than 10,000 emails are received. What kind of sample is this?
4. Every 10 years, the U.S. Census Bureau attempts to count every person living in the United States. To check the accuracy of their count in a certain city, they draw a sample of census districts (roughly equivalent to a city block) and recount everyone in the sampled districts. What kind of sample is formed by the people who are recounted?

Objective 4 Distinguish between statistics and parameters

## Explain It Again

Statistic and parameter: An easy way to remember these terms is that "statistic" and "sample" both begin with "s," and "parameter" and "population" both begin with "p."
5. A public health researcher is designing a study of the effect of diet on heart disease. The researcher knows that the diets of men and women tend to differ, and that men are more susceptible to heart disease. To be sure that both men and women are well represented, the study comprises a simple random sample of 100 men and another simple random sample of 100 women. What kind of sample do these 200 people represent?
6. A college basketball team held a promotion at one of its games in which every twentieth person who entered the arena won a free basketball. What kind of sample do the winners represent?

Answers are on page 12.

## Simple random sampling is the most basic method

Simple random sampling is not the only valid method of random sampling. But it is the most basic, and we will focus most of our attention on this method. From now on, unless otherwise stated, the terms sample and random sample will be taken to mean simple random sample.

## Statistics and Parameters

We often use numbers to describe, or summarize, a sample or a population. For example, suppose that a pollster draws a sample of 500 likely voters in an upcoming election, and $68 \%$ of them say that the state of the economy is the most important issue for them. The quantity " $68 \%$ " describes the sample. A number that describes a sample is called a statistic.

## DEFINITION

A statistic is a number that describes a sample.

Now imagine that the election takes place, and that one of the items on the ballot is a proposition to raise the sales tax to pay for the development of a new park downtown. Let's say that $53 \%$ of the voters vote in favor of the proposition. The quantity " $53 \%$ " describes the population of voters who voted in the election. A number that describes a population is called a parameter.

## DEFINITION

A parameter is a number that describes a population.

## EXAMPLE 1.10 Distinguishing between a statistic and a parameter

Which of the following is a statistic and which is a parameter?
a. $57 \%$ of the teachers at Central High School are female.
b. In a sample of 100 surgery patients who were given a new pain reliever, $78 \%$ of them reported significant pain relief.

## Solution

a. The number $57 \%$ is a parameter, because it describes the entire population of teachers in the school.
b. The number $78 \%$ is a statistic, because it describes a sample.

## USING TECHNOLOGY

We use Example 1.5 to illustrate the technology steps.

## TI-84 PLUS

## Drawing a simple random sample

Step 1. Enter any nonzero number on the HOME screen as the seed.
Step 2. Press STO >
Step 3. Press MATH, select PRB, then 1: rand, and then press ENTER. This enters the seed into the calculator memory. See Figure A, which uses the number 21 as the seed.
Step 4. Press MATH, select PRB, then 5: randInt. Then enter $\mathbf{1 , N}, \mathbf{n}$, where $\mathbf{N}$ is the population size and $\mathbf{n}$ is the desired sample size. In Example 1.5, we use $\mathbf{N}=40$ and $\mathbf{n}=5$ (Figure B).
Step 5. Press ENTER. The five values in the random sample for Example 1.5 are 27, 39, 30, 35, 17 (Figure C).
Note that when using this method, you may sometimes
 get a sample in which a number appears more than once. When this happens, just draw another sample.


Figure A

|  |
| :---: |
|  |

Figure C
$40,5)$
$\{27 \ldots 39 . .30 . .35 .17\}$

